

Y12 Further Mathematics

Revision List for End of Year Exams

| Pure Year 1/AS | | | |
|------------------|---|---|---------------------------------------|
| Chapter 1 | Basic algebraic manipulation, indices and surds | Laws of indices | Pg 2 Ex 1A, Pg 9 Ex 1D |
| | | Expanding brackets, collecting like terms, factorising | Pg 4 Ex 1B, Pg 6 Ex 1C |
| | | Surds | Pg 12 Ex 1E, Pg 13 Ex 1F |
| Chapter 2 | Quadratic Functions | Solving quadratic equations by factorising, quadratic formula | Pg 19 Ex 2A, Pg 20 Ex 2B |
| | | Complete the square | Pg 22 Ex 2C, Pg 24 Ex 2D |
| | | Function notation | Pg 25 Ex 2E |
| | | Quadratic graphs | Pg 27 Ex 2F |
| Chapter 3 | Equations & Inequalities | Linear simultaneous equations | Pg 39 Ex 3A |
| | | Quadratic simultaneous equations | Pg 41 Ex 3B |
| | | Solving simultaneous equations graphically | Pg 42 Ex 3C |
| | | Linear Inequalities | Pg 46 Ex 3D |
| Chapter 5 | Straight Line Graphs | Using the equations of straight line | Pg 90 Ex 5A, Pg 91 Ex 5B, Pg 93 Ex 5C |
| | | Parallel and perpendicular lines | Pg 97 Ex 5E, Pg 98 Ex 5F |
| | | Length and area | Pg 100 Ex 5G |
| | | Modelling with straight lines | Pg 103 Ex 5H |
| Chapter 9 | Trigonometry | Cosine rule | Pg 174 Ex 9A |

| | | | |
|--|---|---|--------------|
| | | Sine rule | Pg 179 Ex 9B |
| | | Ambiguous case | Pg 183 Ex 9C |
| | | Area of a triangle | Pg 185 Ex 9D |
| Chapter 2, 3 | | | |
| Quadratic Functions Equations & Inequalities (prep for circles) | The discriminant | Pg 30 Ex 2G | |
| | Modelling with discriminants | Pg 32 Ex 2H | |
| | Simultaneous Equation recap | Pg 41 Ex 3B | |
| | Quadratic inequalities | Pg 48 Ex 3E | |
| | Solving inequalities graphically | Pg 51 Ex 3F, Pg 53 Ex 3G | |
| | Straight line recap | Pg 90 Ex 5A, Pg91 Ex5B, Pg 93 Ex 5C | |
| Chapter 4 | | | |
| Graphs and transformations | Cubic, quartic and reciprocal graphs | Pg 60 Ex 4A, Pg 64 Ex 4B, Pg66 Ex 4C | |
| | Points of intersection | Pg 68 Ex 4D | |
| | Transforming graphs (translate, stretch, reflect) | Pg 71 Ex 4E, Pg 75 Ex 4F | |
| | Transforming functions | Pg 79 Ex 4G | |
| Chapter 6 | | | |
| Circles | Midpoints and perpendicular bisectors | Pg 114 Ex 6A, Pg 116 Ex 6B | |
| | Equation of a circle | Pg 117 Ex 6c | |
| | Intersection of lines and circles | Pg 121 Ex 6D | |
| | Tangents and chords | Pg 123 Ex 6E | |
| | Circles and triangle | Pg 128 Ex 6F | |
| Chapter 7 | | | |
| Algebraic methods | Algebraic fractions | Pg 138 Ex 7A | |
| | Polynomial division | Pg 139 Ex 7B | |
| | Factor theorem | Pg 143 Ex 7C | |
| | Proof | Pg 146 Ex 7D, Pg 150 Ex 7E | |
| Chapter 8 | | | |
| Binomial theorem | Pascal's triangle | Pg 159 Ex 8A | |
| | Factorial notation | Pg 161 Ex 8B | |
| | Using the binomial theorem | Pg 163 Ex 8C, Pg165 Ex 8D, pg 167 Ex 8D | |

| | | | |
|---------------------|----------------------------------|---|---|
| | | | |
| | | | |
| Chapter 9 | Trigonometric ratios | Cosine rule recap | Pg 174 Ex 9A |
| | | Sine rule recap | Pg 179 Ex 9B |
| | | Ambiguous case recap | Pg 183 Ex 9C |
| | | Area of a triangle recap | Pg 185 Ex 9D |
| | | Problem solving using trigonometry | Pg 187 Ex 9E |
| | | Trigonometric graphs and graph transformations | Pg 192 Ex 9F, Pg194 Ex 9G |
| A2 Chapter 5 | A2**Radians (Introduction) | Radian measure | Pg 114 Ex5A, Pg 117 Ex5B |
| | | Arc Length | Pg 118 Ex5C |
| | | Areas of sectors and segments | Pg 122 Ex5D |
| | | Solving trigonometric equations using radians | Pg 128 Ex5E |
| Chapter 10 | Trig identities and Equations | Angles in all 4 quadrants and trig ratios | Pg 203 Ex 10A, Pg 208 Ex 10B |
| | | Using identities | Pg 209 Ex 10c |
| | | Solving equations | Pg 213 Ex 10D, Pg 217 Ex 10E |
| | | Using identities to solve equations | Pg 219 Ex 10F |
| | | | |
| Chapter 12 | Differentiation | Gradients of chords and differentiation by first principles | Pg 256 Ex 12A, Pg 259 Ex 12B |
| | | Differentiation of functions | Pg 262 Ex 12C, Pg 264 Ex 12D, Pg 266 Ex 12E |
| | | Gradients of tangents and normals | Pg 268 Ex 12F |
| | | Increasing and decreasing functions | Pg 270 Ex 12G |
| | | Second order differentials and stationary points | Pg 271 Ex 12H, Pg 273 Ex 12I |
| | | Sketching gradient functions | Pg 277 Ex 12J |
| | | Modelling with differentiation | Pg 279 Ex 12K |
| | | | |
| Chapter 11 | Vectors | Properties of vectors | Pg 231 Ex 11A |
| | | Representing vectors | Pg 235 Ex 11B |

| | | | |
|----------------------|---------------------------|---|--|
| | | Magnitude and direction | Pg 238 Ex 11C |
| | | Position vectors | Pg 242 Ex 11D |
| | | Solving vector problems | Pg 244 Ex 11E, Pg 248 Ex 7F |
| | | | |
| A2 Chapter 12 | A2** Vectors | 3D Co-ordinates and 3D vectors | Pg 337 Ex 12A |
| | | Solving geometric problems | Pg 344 Ex 12B |
| | | | |
| Chapter 13 | Integration | Basic integration | Pg 288 Ex13A, Pg 290 Ex13B |
| | | Finding functions | Pg 293 Ex13C |
| | | Definite integrals | Pg 295 Ex13D |
| | | Areas under curves and between curves and lines | Pg 297 Ex13E, Pg 300 Ex13F, Pg 302 Ex13G |
| | | | |
| Chapter 14 | Exponentials & Logarithms | Exponential functions | Pg 312 Ex 14A |
| | | $y = e^x$ | Pg 314 Ex14B |
| | | Exponential functions | Pg 316 Ex14C |
| | | Logarithms, laws of logs and solving equations | Pg 318 - 324 Ex14D - F |
| | | Natural logarithms | Pg 326 Ex14G |
| | | Logarithms and non-linear data | Pg 328 Ex14H |
| | | | |

| Applied Stats Year 1/AS | | | |
|-------------------------|------------------------------|--|------------------------|
| Chapter 1 | The Large Data Set | Large Data Set introduction in computer room | LDS Summary page |
| Chapter 1 | Data Collection | Population and samples | Pg 2Ex1A |
| | | Sampling | Pg 4 Ex1B, Pg 7 Ex 1C |
| | | Types of data | Pg 9 Ex1D |
| | | Large data set | Pg 11 Ex1E |
| Chapter 2 | Measure of location & spread | Measures of central tendency (mean, mode, median) | Pg 21 Ex2A, Pg 24 Ex2B |
| | | Other measures of location (quartiles and percentiles) | Pg 25 Ex2C |
| | | Measures of spread | Pg 28 Ex2D |
| | | Variance and standard deviation | Pg 30 Ex2E |
| | | Coding | Pg 33 Ex2F |
| | | | |
| Chapter 3 | Representation of data | Outliners and boxplots | Pg 41 Ex3A, Pg 43 Ex3B |
| | | Cumulative frequency | Pg 46 Ex3C |
| | | Histograms | Pg 48 Ex3D |
| | | Comparing data | Pg 53 Ex3E |
| | | | |
| Chapter 5 | Probability | Calculating probabilities | Pg 70 Ex5A |
| | | Venn diagrams | Pg 72 Ex5B |
| | | Mutually exclusive and independent events | Pg 75 Ex5C |
| | | Tree diagrams | Pg 78 Ex5D |
| A2 Chapter 2 | Conditional probability | Set notation | Pg 17 Ex2A |
| | | Conditional probability | Pg 21 Ex2B |

| | | | |
|-----------|---------------------------|---------------------------|------------------------|
| | | Venn diagrams | Pg 24 Ex2C |
| | | Probability formulae | Pg 27 Ex2D |
| | | Tree diagrams | Pg 31 Ex2E |
| | | | |
| Chapter 6 | Statistical distributions | Probability distributions | Pg84 Ex6A |
| | | Binomial distributions | Pg 88 Ex6B, Pg 91 Ex6C |
| | | | |
| Chapter 7 | Hypothesis Testing | Hypothesis Testing | Pg 99 Ex7A |
| | | Finding critical regions | Pg 101 Ex7B |
| | | One tailed tests | Pg 105 Ex7C |
| | | Two tailed tests | Pg 107 Ex7D |
| | | | |

| Applied Further Stats Year 1/AS | | | |
|--|---------------------------|---|-------|
| Chapter 1 | Discrete Random Variables | Expected value of a discrete random variable | Pg 2 |
| | | Variance of a discrete random variable | Pg 5 |
| | | Expected value and variance of a function of x | Pg 7 |
| | | Solving problems involving random variables | Pg 11 |
| | | | |
| Chapter 2 | Poisson Distribution | The Poisson Distribution | Pg 20 |
| | | Modelling with Poisson | Pg 23 |
| | | Adding Poisson distributions | Pg 27 |
| | | Mean & Variance of Poisson | Pg 30 |
| | | Mean & Variance of Binomial | Pg 32 |
| | | Using the Poisson distribution to approx. the binomial distribution | Pg 34 |
| | | | |
| Chapter 4 | Hypothesis Testing | Testing for the mean of a Poisson distribution | Pg 59 |

| | | | |
|------------------|-------------------|--|--------|
| | | Finding critical regions for a Poisson distribution | Pg 62 |
| Chapter 6 | Chi-squared tests | Goodness of Fit | Pg 92 |
| | | Degrees of freedom & the chi-squared family of distributions | Pg 96 |
| | | Testing a hypothesis | Pg 99 |
| | | Testing the goodness of fit with discrete data | Pg 103 |
| | | Using contingency tables | Pg 113 |

| Applied Mechanics Year 1/AS | | | |
|------------------------------------|------------------------|--|----------------------------|
| Chapter 8 | Modelling in Mechanics | Constructing a model and modelling assumptions | Pg 118 Ex 8A, Pg 120 Ex 8B |
| | | Quantities and units | Pg 122 Ex 8c |
| | | Working with vectors | Pg 125 Ex 8D |
| Chapter 9 | Constant acceleration | Displacement time graphs | Pg 130 Ex9A |
| | | Velocity time graphs | Pg 133 Ex9B |
| | | Constant acceleration (suvat) formulae | Pg 137 Ex9C, Pg 142 Ex 9D |
| | | Vertical motion under gravity | Pg 146 Ex9E |
| Chapter 10 | Forces & Motion | Forces diagrams | Pg 156 Ex10A |
| | | Forces as vectors | Pg 160 Ex10B |
| | | Forces and acceleration | Pg 162 Ex10C |
| | | Motion in 2 dimensions | Pg 166 Ex10D |
| | | Connected particles and pulleys | Pg 169 Ex10E, Pg 173 Ex10F |
| A2 Chapter 5 | Forces & Friction | Resolving forces | Pg 91 Ex5A |
| | | Inclined planes | Pg 96 Ex5B |
| | | Friction | Pg 100 Ex5C |

| | | | |
|---------------------|-----------------------|---|-----------------------------|
| A2 Chapter 7 | Application of forces | Static particles – excluding moments | Pg 129 Ex7A, Pg 133 Ex7B |
| | | Friction and static particles | Pg137 Ex7C |
| | | Dynamic and inclined planes | Pg 147 Ex7E |
| | | Connected particles | Pg 150 Ex7F |
| | | | |
| Chapter 11 | Variable acceleration | Functions of time | Pg 182 Ex11A |
| | | Using differentiation, maxima and minima problems | Pg 185 Ex11B, Pg 186 Ex 11C |
| | | Using Integration | Pg 188 Ex11D |
| | | Constant acceleration (suvat) formulae | Pg 191 Ex11E |
| | | | |

| Applied Further Mechanics Year 1/AS | | | |
|--|------------------------|---|-------|
| Chapter 1 | Momentum and impulse | Momentum in one direction | Pg 2 |
| | | Conservation of momentum | Pg 4 |
| | | Momentum as a vector (A2 content, taught in Y12) | Pg 9 |
| | | | |
| Chapter 2 | Work, Energy and Power | Work done | Pg 16 |
| | | Kinetic and potential energy | Pg 20 |
| | | Conservation of mechanical energy & the work-energy principle | Pg 24 |
| | | Power | Pg 29 |
| | | | |
| Chapter 4 | Elasticity | Direct impact & Newton's law of restitution | Pg 70 |
| | | Direct collision with a smooth plane | Pg 76 |
| | | Loss of kinetic energy | Pg 79 |
| | | Successive direct impacts | Pg 84 |
| | | | |

| AS Further Maths Core Year 1/AS | | | |
|---------------------------------|-----------------------|---|--------|
| Chapter 1 | Complex Numbers | Imaginary and complex numbers | Pg 2 |
| | | Multiplying complex numbers | Pg 5 |
| | | Complex conjugation | Pg 5 |
| | | Roots of quadratic equations | Pg 10 |
| Chapter 2 | Argand Diagrams | Argand diagrams | Pg 18 |
| | | Modulus and argument | Pg 20 |
| | | Modulus-argument form of complex numbers | Pg 23 |
| | | Loci in the Argand diagram | Pg 28 |
| | | Regions in the Argand diagram | Pg 36 |
| Chapter 3 | Series | Sums of natural numbers | Pg 44 |
| | | Sums of squares and cubes | Pg 45 |
| | | | |
| Chapter 4 | Roots of Polynomials | Roots of a quadratic equation | Pg 55 |
| | | Roots of a cubic equation | Pg 57 |
| | | Roots of a quartic equation | Pg 59 |
| | | Expressions relating to the roots of a polynomial | Pg 62 |
| | | Linear Transformations of roots | Pg 65 |
| Chapter 5 | Volumes of Revolution | Around the x axis | Pg 72 |
| | | Around the y axis | Pg 76 |
| | | Adding and subtracting volumes | Pg 78 |
| | | Modelling with volumes of revolution | Pg 83 |
| | | | |
| Chapter 6 | Matrices | Introduction to matrices | Pg 95 |
| | | Matrix multiplication | Pg 99 |
| | | Determinants | Pg 104 |
| | | Inverting a 2 x 2 matrix | Pg 108 |
| | | Inverting a 3 x 3 matrix | Pg 112 |
| | | Solving systems of equations using matrices | Pg 116 |

| | | | |
|------------------|------------------------|---|--|
| | | | |
| Chapter 7 | Linear Transformations | Linear transformations in two dimensions Reflections and rotations Enlargements and stretches Successive transformations Linear transformations in 3D The inverse of a linear transformation | Pg 127 Pg 131 Pg 136 Pg 140 Pg 144 Pg 148 |
| Chapter 8 | Proof by Induction | Proof by mathematical induction Proving divisibility results Proving statements involving matrices | Pg 156 Pg 160 Pg 162 |
| Chapter 9 | Vectors | Equation of a line in 3D Equation of a plane in 3D Scalar product Calculating angles between lines and planes Points of intersection Finding perpendiculars | Pg 168 Pg 175 Pg 178 Pg 184 Pg 189 Pg 193 |
| | | | |