

# A Level DT Maths lessons

**Red text** and boxes indicate the correct methods of working out and the answers

# AQA specification (content to be learnt for the exam)

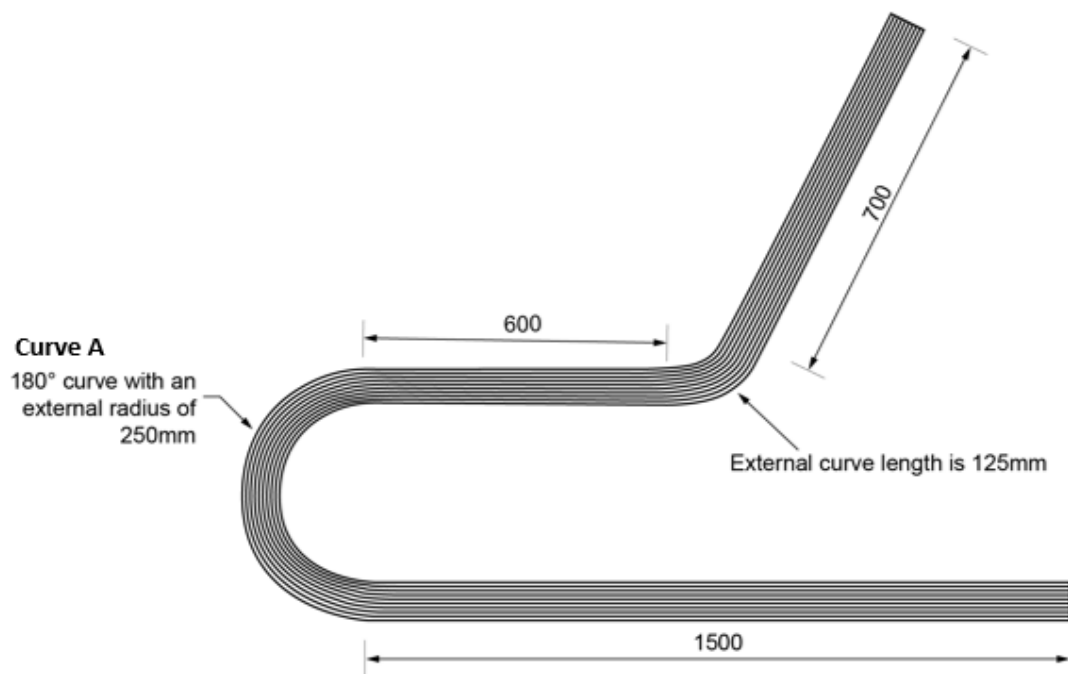
## 7.1 Maths

Ref	Maths skills requirement	Potential applications: product design
a	Confident use of number and percentages	Calculation of quantities of materials, costs and sizes
b	Use of ratios	Scaling drawings
c	Calculation of surface areas and/or volumes	Determining quantities of materials
d	Use of trigonometry	Calculation of sides and angles as part of product design
e	Construction, use and/or analysis of graphs and charts	Representation of data used to inform design decisions and evaluation of outcomes.  Presentation of market data, user preferences, outcomes of market research
f	Use of coordinates and geometry	Use of datum points and geometry when setting out design drawings
g	Use of statistics and probability as a measure of likelihood	Interpret statistical analyses to determine user needs and preferences.  Use data related to human scale and proportion to determine product scale and dimensions

# First Question

7. A lounge chair is to be manufactured by laminating seven layers of 1.5mm thick, 100mm wide ash veneer together to form each side of the chair frame.

**Figure 1** below shows detail of the side profile for each side frame used in the assembly of the chair.



**Figure 1**

- (a) The manufacturer cuts all seven veneers to the same length; the sum of the chair's three straight sections, added to the length of both external curves. Assume no excess will be needed for trimming on the width of the laminated framework.

- i) Determine the length of the external curve A shown in **Figure 1**.  
Give your answer to the nearest whole number.

**[3 marks]**

**7. Award marks as stated**

(a) Mathematical calculations

i)

**[3 marks]**

1 mark	Use of correct formula and correct substitution: Circumference of external curve as a full circle $C = \pi \times D$ $C = \pi \times 500$ , or $2 \times \pi \times 250$ $C = 1,571 \text{ mm (or equivalent)}$
1 mark	Length of 180° of external curve: $180 / 360 \times 100 = 50\%$ of full circle circumference
1 mark	Length of external curve: $1,571 \times 50 / 100 = 785.5 \text{ mm. Rounded to } 786\text{mm.}$

7. Award marks as stated

(a) Mathematical calculations

i)

[3 marks]

1 mark	Use of correct formula and correct substitution: Circumference of external curve as a full circle $C = \pi \times D$ $C = \pi \times 500$ , or $2 \times \pi \times 250$ $C = 1,571 \text{ mm}$ (or equivalent)
1 mark	Length of $180^\circ$ of external curve: $180 / 360 \times 100 = 50\%$ of full circle circumference
1 mark	Length of external curve: $1,571 \times 50 / 100 = 785.5 \text{ mm}$ . Rounded to 786mm.

- ii) Determine the total length of veneer used in the construction of the **two** side frames for the chair. **[2 marks]**

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- (b) Ash veneer for constructional purposes retails at £20.45 per metre square (m<sup>2</sup>). Calculate the cost of the veneer needed to manufacture two side frames for the chair. Include an additional 15% of veneer to allow for waste/trimming. Give your answer in pounds and pence. **[2 marks]**

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ii)		[2 marks]
1 mark	Adding component lengths together: $1500 + 786 + 600 + 125 + 700 = 3,711 \text{ mm}$	
1 mark	Two side frames each with 7 veneers: $3711 \times 7 \times 2 = 51,954 \text{ mm}$ . Accept answer in metres e.g. 51.95m	
(b) Mathematical calculations		[2 marks]
1 mark	Area of veneer: $51.95\text{m} \times 0.1\text{m wide} = 5.195 \text{ m}^2$ Plus 15 %: $5.195 \times 1.15 = 5.97425 = 5.97 \text{ m}^2$	
1 mark	$\text{£}20.45 \times 5.97 = 122.0865 = \text{£}122.09$	

ii) **[2 marks]**

1 mark	Adding component lengths together: $1500 + 786 + 600 + 125 + 700 = 3,711 \text{ mm}$
1 mark	Two side frames each with 7 veneers: $3711 \times 7 \times 2 = 51,954 \text{ mm}$ . Accept answer in metres e.g. 51.95m

(b) Mathematical calculations **[2 marks]**

1 mark	Area of veneer: $51.95\text{m} \times 0.1\text{m wide} = 5.195 \text{ m}^2$ Plus 15 %: $5.195 \times 1.15 = 5.97425 = 5.97 \text{ m}^2$
1 mark	$\text{£}20.45 \times 5.97 = 122.0865 = \text{£}122.09$

Next Question – Box Plots



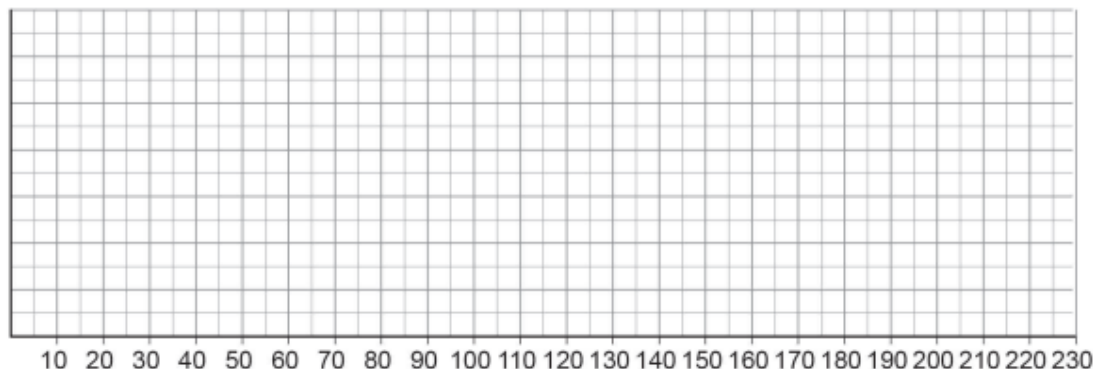
**0 4** The battery life of a rechargeable battery was tested in a handheld electronic device. The test was repeated 11 times with a new battery each time.

The results are shown in the table below.

	1	2	3	4	5	6	7	8	9	10	11
Battery life (in minutes)	65	110	180	130	90	220	150	75	90	190	210

On the grid below draw a box plot to show the results.

**[4 marks]**



<https://corbettmaths.com/wp-content/uploads/2013/02/box-plots-pdf.pdf>

<https://corbettmaths.com/2013/05/15/drawing-and-reading-box-plots/>

4

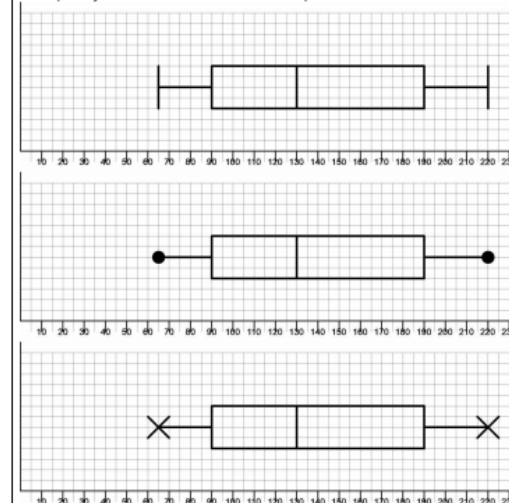
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On the grid below draw a box plot to show the results.

	1	2	3	4	5	6
Battery Life (in minutes)	65	110	180	130	90	220
	7	8	9	10	11	
Battery Life (in minutes)	150	75	90	190	210	

Calculate of median	130	B1 (Value seen) (written or plotted)
Calculate Lower quartile	90	B2 (Value seen) (written or plotted)
Calculate upper quartile	190	B3 (Value seen) (written or plotted)
Correct box plot	SEE Box plot below	A1 (follow through)
For the correct box plot award full marks		4 marks

Accept any of the three alternative box plots:



4 marks

AO42C

Next Question - Probability

**0 5** When producing a die cut package, three different, independently occurring faults are possible with these probabilities:

**Fault A:** 1/100

**Fault B:** 1/100

**Fault C:** 1/500

**A** and **B** are minor faults which must be monitored but will only fail quality control if both faults are seen on a single product.

**C** is a critical fault and any product suffering from this fault will fail quality control.

If a batch of 10 000 packages are produced, calculate how many products would be expected to fail quality control.

**[3 marks]**

<https://corbettmaths.com/wp-content/uploads/2014/08/probability-pdf.pdf>

5	<p>When producing a die cut package three different, independently occurring faults are possible with these probabilities:</p> <p><b>Fault A:</b> 1/100 <b>Fault B:</b> 1/100 <b>Fault C:</b> 1/500</p> <p><b>A</b> and <b>B</b> are minor faults which must be monitored but will only fail Quality Control if both faults are seen on a single product.</p> <p><b>C</b> is a critical fault and any product suffering from this fault will fail quality control.</p> <p>If a batch of 10 000 packages are produced, calculate how many products would be expected to fail quality control.</p> <table><tr><td>Calculate probability of Fault A and B</td><td><math>1/100 \times 1/100</math> or <math>0.01 \times 0.01 = 1/10000</math> or <math>0.0001</math></td><td>M1</td></tr><tr><td>Calculate probability of Fault A and B or C</td><td><math>1/100 \times 1/100 + 1/500 = 21/10000</math> or <math>0.01 \times 0.01 + 0.005 = 0.0021</math> or <math>2.1 \times 10^{-3}</math> <math>1/10000 + 1/500 = 21/10000</math></td><td>M2</td></tr><tr><td>Calculate expected number of failures</td><td>21 products or 21</td><td>M3</td></tr><tr><td>For the correct answer award full marks</td><td></td><td>3 marks</td></tr></table>	Calculate probability of Fault A and B	$1/100 \times 1/100$ or $0.01 \times 0.01 = 1/10000$ or $0.0001$	M1	Calculate probability of Fault A and B or C	$1/100 \times 1/100 + 1/500 = 21/10000$ or $0.01 \times 0.01 + 0.005 = 0.0021$ or $2.1 \times 10^{-3}$ $1/10000 + 1/500 = 21/10000$	M2	Calculate expected number of failures	21 products or 21	M3	For the correct answer award full marks		3 marks	3 marks	AO42C
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For the correct answer award full marks		3 marks													

5

When producing a die cut package three different, independently occurring faults are possible with these probabilities:

**Fault A:** 1/100

**Fault B:** 1/100

**Fault C:** 1/500

**A** and **B** are minor faults which must be monitored but will only fail Quality Control if both faults are seen on a single product.

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If a batch of 10 000 packages are produced, calculate how many products would be expected to fail quality control.

Calculate probability of Fault A and B	$1/100 \times 1/100$ or $0.01 \times 0.01 = 1/10000$ or $0.0001$	M1
Calculate probability of Fault A and B or C	$1/100 \times 1/100 + 1/500 = 21/10000$ or $0.01 \times 0.01 + 0.005 = 0.0021$ or $2.1 \times 10^{-3}$ $1/10000 + 1/500 = 21/10000$	M2
Calculate expected number of failures	21 products or 21	M3
For the correct answer award full marks		3 marks

3 marks

AO42C

Next Question - Volumes

**1 2** **Figure 4** shows a low carbon steel component with a volume of  $11\,100\text{ mm}^3$

The density of low carbon steel is  $7.85\text{ g/cm}^3$

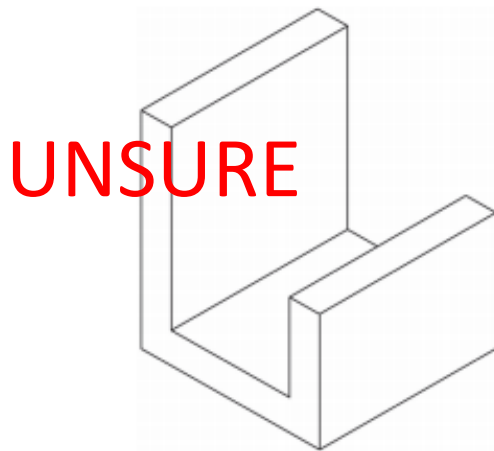
The component is to be hot dip galvanised.

The galvanising process increases the mass of the component by 5%

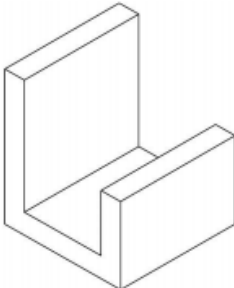
Calculate the mass of the galvanised component in grams.

Show your working out.

**Figure 4**  
**Isometric view**



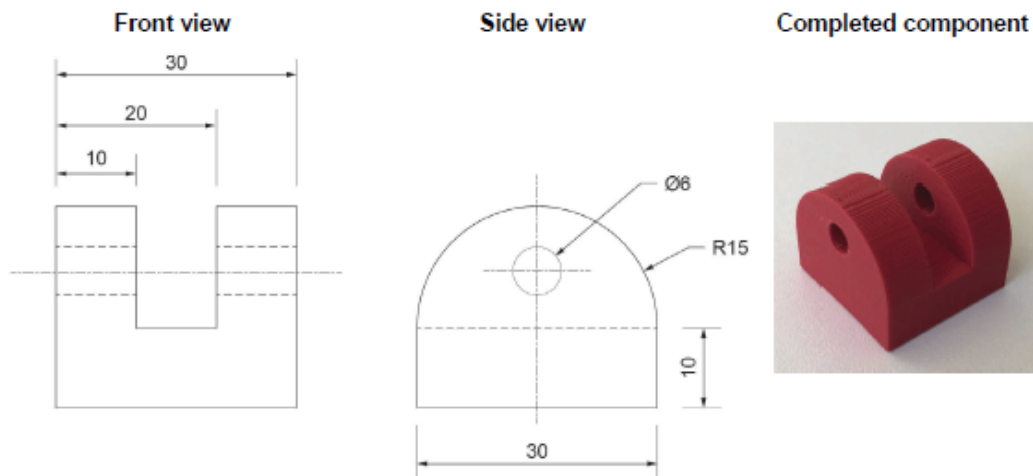
**[3 marks]**

12	<p><b>Figure 4</b> shows a low carbon steel component with a volume of <math>11\,100\text{ mm}^3</math></p> <p>The density of low carbon steel is <math>7.85\text{ g/cm}^3</math></p> <p>The component is to be hot dip galvanised.</p> <p>The galvanising process increases the mass of the component by 5%</p> <p>Calculate the mass of the galvanised component in grams.</p> <p>Show your working out.</p> <p style="text-align: center;"><b>Figure 4</b> <b>Isometric view</b></p>  <table border="1"> <tr> <td>Conversion of density into <math>\text{g/mm}^3</math> or Conversion of volume into <math>\text{cm}^3</math></td><td><math>7.85\text{ g/cm}^3 = 0.00785\text{ g/mm}^3</math> or <math>7.85 \times 10^{-3}</math> or <math>11\,100 = 11.1\text{ cm}^3</math></td><td>M1</td></tr> <tr> <td>Calculate the mass prior to galvanising (application of volume x density calculation)</td><td><math>11\,100 \times \text{their } 0.00785 = \text{their } 87.135\text{ grams}</math></td><td>M2</td></tr> <tr> <td>Calculate the mass once galvanised</td><td><math>87.135 \times 1.05 = [91, 91.5]\text{ grams}</math></td><td>A1</td></tr> <tr> <td colspan="2">For the correct answer award full marks</td><td>3 marks</td></tr> </table>	Conversion of density into $\text{g/mm}^3$ or Conversion of volume into $\text{cm}^3$	$7.85\text{ g/cm}^3 = 0.00785\text{ g/mm}^3$ or $7.85 \times 10^{-3}$ or $11\,100 = 11.1\text{ cm}^3$	M1	Calculate the mass prior to galvanising (application of volume x density calculation)	$11\,100 \times \text{their } 0.00785 = \text{their } 87.135\text{ grams}$	M2	Calculate the mass once galvanised	$87.135 \times 1.05 = [91, 91.5]\text{ grams}$	A1	For the correct answer award full marks		3 marks	3 marks
Conversion of density into $\text{g/mm}^3$ or Conversion of volume into $\text{cm}^3$	$7.85\text{ g/cm}^3 = 0.00785\text{ g/mm}^3$ or $7.85 \times 10^{-3}$ or $11\,100 = 11.1\text{ cm}^3$	M1												
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Calculate the mass once galvanised	$87.135 \times 1.05 = [91, 91.5]\text{ grams}$	A1												
For the correct answer award full marks		3 marks												

Next Question – Volumes, Mass and  
Density

0 8 Figure 4 shows the dimensions of a component to be made using 3D printing.

**Figure 4**  
All dimensions in mm  
Not drawn to scale



Material costs		
Material	Printed density (grams per mm <sup>3</sup> )	Cost per 500 g
ABS	0.000 448 g	£18

Calculate the material cost of manufacturing 50 units.

Show your working out.

[5 marks]

8	<p><b>Figure 4</b> shows the dimensions of a component to be made using 3D printing. (Shown in Question Paper)</p> <p>Calculate the material cost of manufacturing 50 units.</p> <table><tr><td><b>Cuboid Volume</b></td><td><math>30 \times 30 \times 10</math> <math>= 9000 \text{ mm}^3</math></td><td>1 mark (M1)</td></tr><tr><td><b>Cross Section of semi circle</b></td><td><math>\frac{1}{2} \times \pi \times 15^2 - \pi \times 3^2</math> <math>= 103.5 \pi</math>  Or  <math>= 353.25 - 28.26</math>  <math>= [324.99, 325.197]</math></td><td>1 mark (M1)</td></tr><tr><td><b>Total Volume</b></td><td>Cross section <math>\times</math> 20 + base  Their <math>[324.99, 325.197] \times 20</math> <math>+ 9000</math>  <math>= [15499.8, 15503.94]</math></td><td>1 mark (A1)</td></tr><tr><td><b>Mass of Shape</b></td><td>Density <math>\times</math> Volume <math>0.000448 \times \text{their } [15499.8, 15503.94] \text{ mm}^3</math> <math>= [6.944, 6.946 \text{ g}]</math></td><td>1 mark (M1)</td></tr><tr><td><b>Cost of 50 units</b></td><td>mass <math>\times</math> 50 units their <math>[6.944, 6.946\text{g}] \times 50</math> <math>= [347.26, 347.3] / 500\text{g} \times 18</math> <math>= \text{£}12.50</math></td><td>1 mark (A1)</td></tr><tr><td><b>Cost of 50 units</b> Where no working has been shown but final answer is accurate</td><td><math>= \text{£}12.50</math></td><td>5 marks</td></tr></table>	<b>Cuboid Volume</b>	$30 \times 30 \times 10$ $= 9000 \text{ mm}^3$	1 mark (M1)	<b>Cross Section of semi circle</b>	$\frac{1}{2} \times \pi \times 15^2 - \pi \times 3^2$ $= 103.5 \pi$  Or  $= 353.25 - 28.26$  $= [324.99, 325.197]$	1 mark (M1)	<b>Total Volume</b>	Cross section $\times$ 20 + base  Their $[324.99, 325.197] \times 20$ $+ 9000$  $= [15499.8, 15503.94]$	1 mark (A1)	<b>Mass of Shape</b>	Density $\times$ Volume $0.000448 \times \text{their } [15499.8, 15503.94] \text{ mm}^3$ $= [6.944, 6.946 \text{ g}]$	1 mark (M1)	<b>Cost of 50 units</b>	mass $\times$ 50 units their $[6.944, 6.946\text{g}] \times 50$ $= [347.26, 347.3] / 500\text{g} \times 18$ $= \text{£}12.50$	1 mark (A1)	<b>Cost of 50 units</b> Where no working has been shown but final answer is accurate	$= \text{£}12.50$	5 marks	5 marks	AO41C
<b>Cuboid Volume</b>	$30 \times 30 \times 10$ $= 9000 \text{ mm}^3$	1 mark (M1)																			
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<b>Cost of 50 units</b>	mass $\times$ 50 units their $[6.944, 6.946\text{g}] \times 50$ $= [347.26, 347.3] / 500\text{g} \times 18$ $= \text{£}12.50$	1 mark (A1)																			
<b>Cost of 50 units</b> Where no working has been shown but final answer is accurate	$= \text{£}12.50$	5 marks																			



Next Question -

1 1 Figure 5 shows an aluminium seat clamp. Figure 6 shows the dimensions of a block of aluminium.

Figure 5

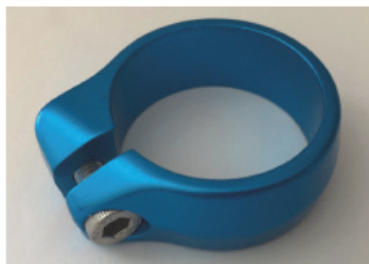
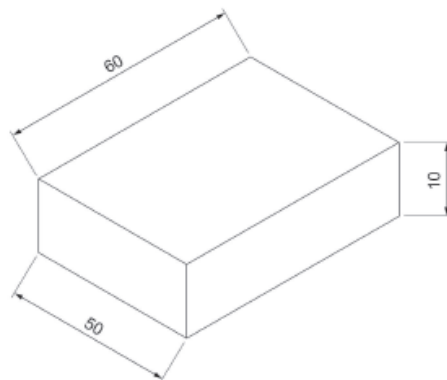


Figure 6  
All dimensions in mm  
Not drawn to scale



The seat clamp is currently manufactured by wastage from the aluminium block shown in Figure 6.

The manufacturer wants to produce the clamp using a redistribution process.

Compare the cost of each manufacturing process if 5000 units are to be produced.

Show your working out.

Volume of the seat clamp	7280 mm <sup>3</sup>
Cost of aluminium	£4 per 100 000 mm <sup>3</sup>
Cost of manufacturing a mould for the redistribution process	£3000

[6 marks]

11

Figure 5 shows an aluminium seat clamp. Figure 6 shows the dimensions of a block of aluminium. (Shown in the Question Paper)

Compare the cost of each manufacturing process if 5000 units are to be produced.

Show your working out.

The volume of the seat clamp	7280 mm <sup>3</sup>
The cost of aluminium	£4 per 100 000 mm <sup>3</sup>
The cost of manufacturing a mould for the redistribution process	£3000

#### Machined seat clamp

Block volume	$10 \times 50 \times 60$ $= 30\,000\text{ mm}^3$	1 mark (M1)
Recognition of correct equation	Block volume + cost of aluminium	1 mark (M1)
Cost for one machined seat clamp	Their $30\,000 + 100\,000 \times £4$ $= £1.20$ per clamp	1 mark (M1)
Cost of 5000 machined seat clamps	Their $1.20 \times 5000$ $= £6000$	1 mark (A1)
Cost of 5000 machined seat clamps Where no working has been shown but final answer is accurate	£6000	4 marks

#### Redistribution seat clamp

Cost for one redistribution seat clamp (without mould factored in)	$7280 \div 100\,000 \times 4$ $= [£0.29, £0.292]$	1 mark (A1)
Cost of 5000 redistribution seat clamps	Their $[£0.29, £0.292] \times 5000 + 3000$ $= [£4450, £4460]$	1 mark (A1)
Cost of 5000 redistribution seat	$= [£4450, £4460]$	2 marks

6 marks

AO41C

Next Question – Volumes and cost

- 1 5 A manufacturer is producing a glass reinforced plastic (GRP) moulding.

Calculate the volume of hardener needed.

Show all of your working.

Size of GRP mat needed for moulding	2 metres × 5 metres
Ratio of resin to hardener	3 : 2
Total volume of liquid (resin and hardener) needed per m <sup>2</sup> of GRP matting	3 litres per m <sup>2</sup>

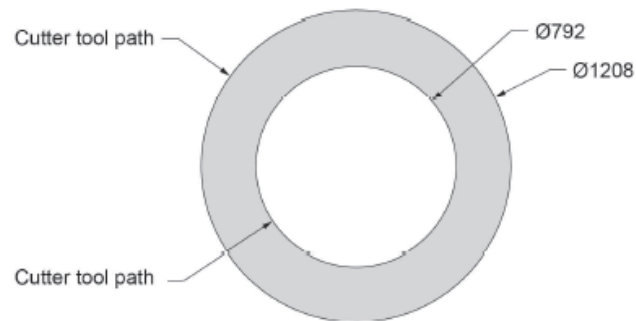
[4 marks]

15	<p>A manufacturer is producing a glass reinforced plastic (GRP) moulding.</p> <p>Calculate the volume of hardener needed.</p> <p>Show all of your working.</p> <table><tr><td>Size of GRP mat needed for moulding</td><td>2 metres × 5 metres</td></tr><tr><td>Ratio of resin to hardener</td><td>3 : 2</td></tr><tr><td>Total volume of liquid (resin and hardener) needed per m<sup>2</sup> of GRP matting</td><td>3 litres per m<sup>2</sup></td></tr></table> <table><tr><td><b>Area of Matting</b></td><td>2 × 5 = 10m<sup>2</sup></td><td>1 mark (M1)</td></tr><tr><td><b>Total volume of liquid needed</b></td><td>10 × 3 = 30 litres</td><td>1 mark (A1)</td></tr><tr><td><b>Ratio factor</b></td><td>3 + 2 = 5 parts 30 ÷ 5 = 6 litres</td><td>1 mark (M1)</td></tr><tr><td><b>Hardener needed</b></td><td>6l × 2 = 12 litres of hardener</td><td>1 mark (A1)</td></tr><tr><td><b>Volume of hardener needed</b> Where no working has been shown but final answer is accurate</td><td>= 12 litres of hardener</td><td>4 marks</td></tr></table>	Size of GRP mat needed for moulding	2 metres × 5 metres	Ratio of resin to hardener	3 : 2	Total volume of liquid (resin and hardener) needed per m <sup>2</sup> of GRP matting	3 litres per m <sup>2</sup>	<b>Area of Matting</b>	2 × 5 = 10m <sup>2</sup>	1 mark (M1)	<b>Total volume of liquid needed</b>	10 × 3 = 30 litres	1 mark (A1)	<b>Ratio factor</b>	3 + 2 = 5 parts 30 ÷ 5 = 6 litres	1 mark (M1)	<b>Hardener needed</b>	6l × 2 = 12 litres of hardener	1 mark (A1)	<b>Volume of hardener needed</b> Where no working has been shown but final answer is accurate	= 12 litres of hardener	4 marks	4 marks	AO41C
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<b>Volume of hardener needed</b> Where no working has been shown but final answer is accurate	= 12 litres of hardener	4 marks																						

Next question -

Figure 10 shows a component to be cut on a computer numerically controlled (CNC) router.

Figure 10  
All dimensions in mm  
Not drawn to scale



Material	Depth of cut per pass	Rate of cut
12 mm MDF	6 mm	6 metres per minute
12 mm plywood	4 mm	4.5 metres per minute

Calculate how long it would take to machine the shape in each of the materials.

Show your working out.

[6 marks]

[illegible]

Next question -

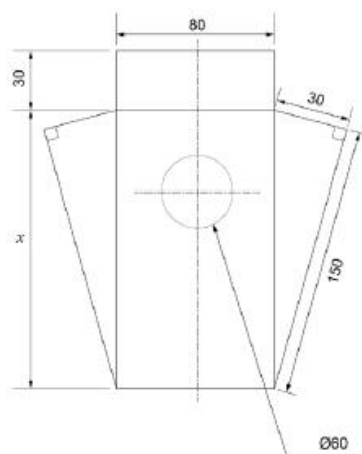
0 2

Figure 1 shows an image of a ceiling light.  
Figure 2 shows the aluminium sheet net made for this light.

Figure 1



Figure 2



All dimensions in mm  
Not to scale

0 2 . 1

Calculate the length of side X.

Show your answer to two decimal places.

[2 marks]

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0 2 . 2

Calculate the surface area of the net shown in Figure 2, with the circular hole removed.

Show your answer to two decimal places.

[3 marks]

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0 2 . 3

Calculate the percentage reduction in surface area caused when the circular hole was cut out.

Show your answer to two decimal places.

[2 marks]

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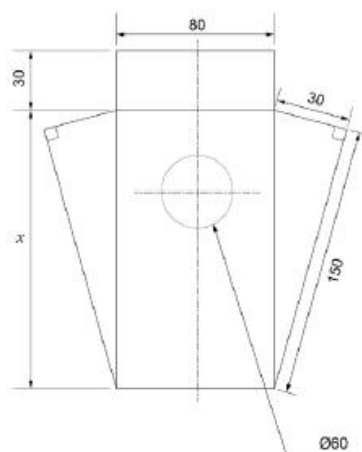
0 2

Figure 1 shows an image of a ceiling light.  
Figure 2 shows the aluminium sheet net made for this light.

Figure 1



Figure 2



All dimensions in mm  
Not to scale

AO4 = 1C

Substitute measurements in to Pythagoras theorem equation	$x^2 = 30^2 + 150^2$	1 mark
Correct calculation of side 'x'	$x = 152.97$ (2dp)	1 mark

If the correct answer is seen, award full marks (use wording of live papers)

0 2 . 2

Calculate the surface area of the net shown in Figure.2, with the circular hole removed.  
Show your answer to two decimal places.

[3 marks]

AO4 = 1C

Calculate area of circle	$=\pi r^2$ $=\pi \times (30 \times 30)$ $=2826$ [2826, 2827.8]	1 mark
Calculate area of triangular sides	Area of triangle = $\frac{1}{2} \times \text{base} \times \text{height}$ $= \frac{1}{2} \times 30 \times 150$ $= 2250$ $2250 \times 2 = 4500$	1 mark
Calculate area of large rectangle	Area of rectangle = $80 \times 152.97$ (or their 2ai) $= 12\,237.6$	
Calculate area of smaller rectangle	Area of rectangle = $80 \times 30$ $= 2400$	
Total area	$= 4500 + 12\,237.6 + 2400 - 2826$ [16 310, 16 311.6]	1 mark

0 2 . 3

Calculate the percentage reduction in surface area caused when the circular hole was cut out.  
Show your answer to two decimal places.

[2 marks]

AO4 = 1C

Set out equation	Percentage area removed = $\frac{\text{Area of circle}}{\text{Area of net}} \times 100\%$	1 mark
Calculate percentage area removed	$= \frac{2827.8}{19\,137.6} \times 100$ =[14.77%, 14.78%]	1 mark

Next question -

CNC coordinates have been used to create the program required to laser cut a part from sheet aluminium.

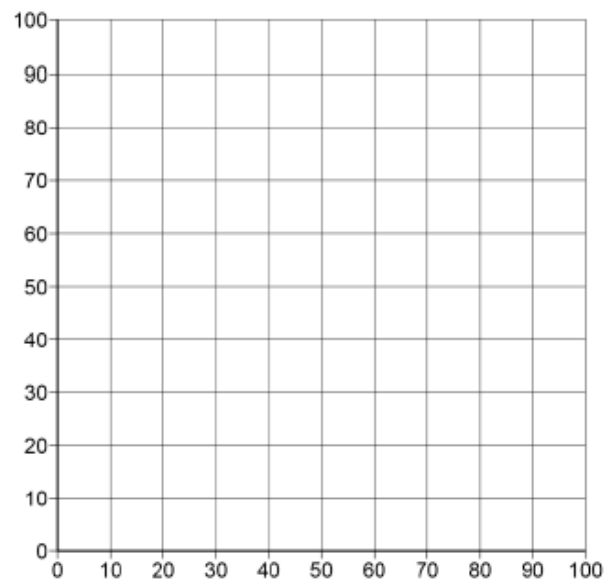
Plot the coordinates on the grid below and use this to calculate the total area of the part.

[5 marks]

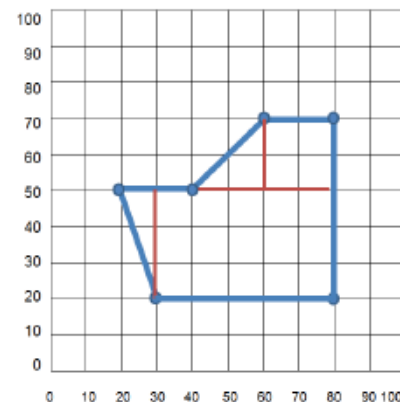
CNC coordinates:

(30,20)  
(80,20)  
(80,70)  
(60,70)  
(40,50)  
(20,50)  
(30,20)

All dimensions in mm



AO4 = 1C



Plot coordinates correctly	See image above	1 mark
Draw lines to define shape	See image above	1 mark
Any rectangular area calculated correctly	e.g. Area1 = $50 \times 30 = 1500$ Area 2 = $20 \times 20 = 400$	1 mark
Any triangular or trapezoidal area calculated correctly	e.g. Area 3 = $\frac{1}{2} \times 10 \times 30 = 150$ Area 4 = $\frac{1}{2} \times 20 \times 20 = 200$ Area of trapezoid = $\frac{a+b}{2} \times h$  = $\frac{60+50}{2} \times 30$  = $1650\text{mm}^2$	1 mark
Calculate total area	Total area = $1500 + 400 + 150 + 200$ = $2250\text{mm}^2$	1 mark

Next question -

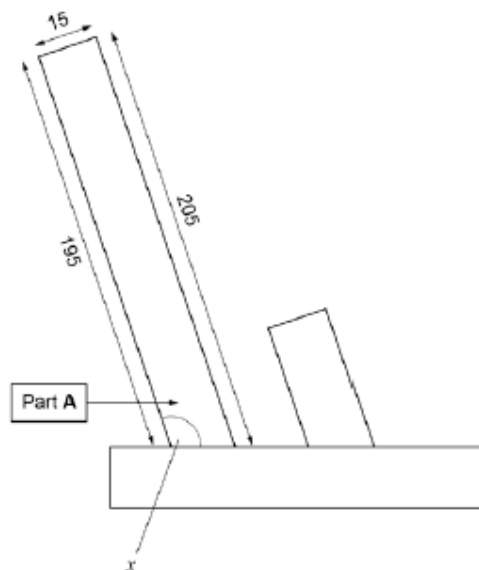
1 0

Figure 7 shows a dimensioned side view of a prototype for a menu holder.

Using the information provided, calculate the angle of  $x$

[4 marks]

Figure 7



All dimensions in mm.  
Not to scale.

1 0

Figure 7 shows a dimensioned side view of a prototype for a menu holder.

Using the information provided, calculate the angle of  $x$

[4 marks]

AO4 = 1C

Set out equation	$\tan a = \text{opposite} \div \text{adjacent}$	1 mark
Substitute values	$\tan a = 15/10$	1 mark
Calculate angle	$a = \tan^{-1} 1.5$ $a = 56.3^\circ$	1 mark
Cutting angle	$180 - 56.3 = 123.7^\circ$	1 mark

Alternative method

Set out equation	$\tan b = \text{opposite} \div \text{adjacent}$	1 mark
Substitute values	$\tan b = 10/15$	1 mark
Calculate angle	$b = \tan^{-1} 0.666$ $b = 33.7^\circ$	1 mark
Cutting angle	$180 - 90 - 33.7 = 56.3^\circ$ $180 - 56.3 = 123.7^\circ$	1 mark

Next Question – Volume of Sphere

Figure 4 shows a tea infuser designed by Marianne Brandt.

Analyse and evaluate how well the tea infuser follows the principles and ethos of the Bauhaus Design School.

[6 marks]

Figure 4

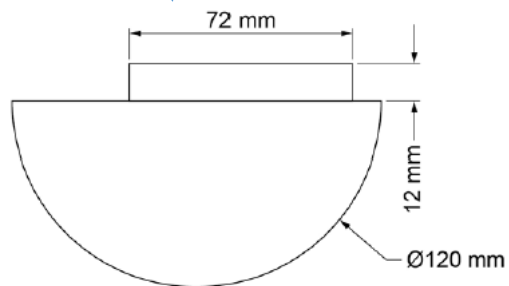


0 2 . 2 The volume of a sphere is  $\frac{4}{3}\pi r^3$

Figure 5 shows a side view of the hemispherical base and cylindrical top section of Marianne Brandt's tea infuser.

Calculate the total volume of these parts of the tea infuser.

Figure 5



[4 marks]

0 2 . 2

The volume of a sphere is  $\frac{4}{3}\pi r^3$

Figure 5 shows a side view of the hemispherical base and cylindrical top section of Marianne Brandt's tea infuser.

Calculate the total volume of these parts of the tea infuser.

[4 marks]

AO4 = 2C

Calculate volume of cylinder	$\pi r^2 h$ $= 3.14 \times 36 \times 36 \times 12$ $= 48\,833.28 \text{ mm}^3$ <p>OR</p> $= 3.142 \times 36 \times 36 \times 12$ $= 48\,864.38 \text{ mm}^3 \text{ (2dp)}$ <p>[48 833.28mm<sup>3</sup>, 48 864.38 mm<sup>3</sup>]</p>	1 mark
Substitute values in to volume of sphere equation	$\frac{2}{3}\pi r^3$ $= \frac{2}{3} \times 3.14 \times (60 \times 60 \times 60)$ <p>OR</p> $\frac{1}{2} \times \frac{4}{3} \pi r^3$ $= \frac{1}{2} \times \frac{4}{3} \times 3.142 \times 60 \times 60 \times 60$	1 mark
Correct volume of hemisphere	[452 160mm <sup>3</sup> , 452 448mm <sup>3</sup> ]	1 mark
Calculate total volume	$48833.28, 48864.38 +$ $452160, 452448$ <p>[500 993.28 mm<sup>3</sup>, 501 312.38 mm<sup>3</sup>]</p>	1 mark

Next question -



0 4 . 1

Figure 6 shows a standing workstation. The ideal height for the desk top is level with the elbow height of the user as shown in Figure 7.

Calculate the range of height adjustment required to accommodate the 15<sup>th</sup> to 85<sup>th</sup> percentiles of the sample shown in Table 1.

[2 marks]

Figure 6



Figure 7

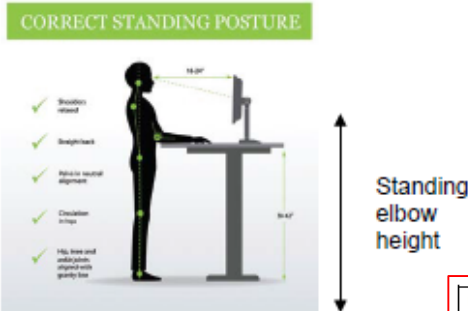


Table 1 shows the ideal elbow height from a range of users.

Standing elbow height	Number in sample
937	5
962	12
987	17
1012	23
1037	30
1062	38
1087	32
1112	26
1137	19
1162	14
1187	4

0 4 . 1

Calculate the range of height adjustment required to accommodate the 15<sup>th</sup> to 85<sup>th</sup> percentiles of the samples shown in Table 1.

[2 marks]

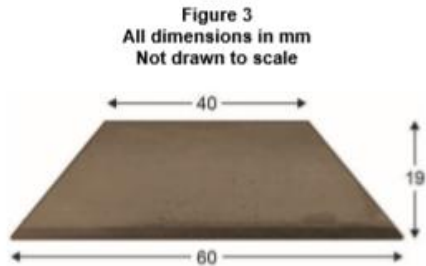
AkO4 = 2C

Calculate 15 <sup>th</sup> percentile	Calculate total in sample = 220  Calculate 15 <sup>th</sup> %ile  $(220 \div 100) \times 15 = 33$	1 mark
Calculate 85 <sup>th</sup> percentile	Calculate 85 <sup>th</sup> %ile  $(220 \div 100) \times 85 = 187$	
Give maximum and minimum heights based on data from original table	Range from 987mm to 1137mm  or 150mm with working seen.	1 mark

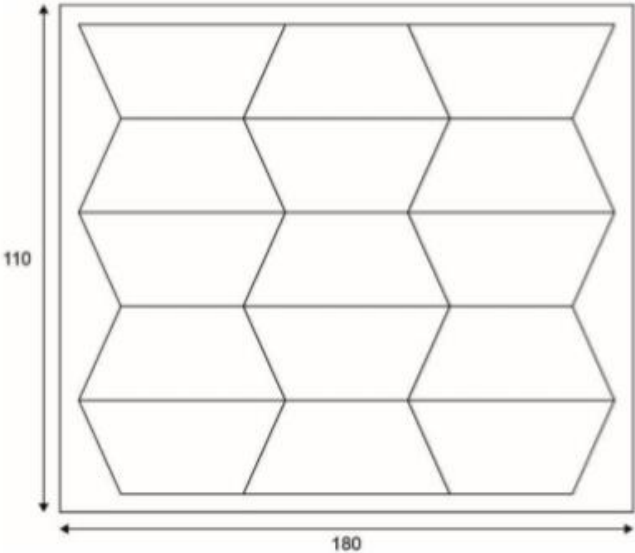
# Next Question

07.1 Figure 3 shows a craft knife blade.

The craft knife blade is manufactured from stainless steel in the shape of a trapezium.



The craft knife blades are cut from a sheet of stainless steel:



Calculate the percentage of the sheet that is wasted when **15** craft knife blades have been cut out.

Show your working out.

[3 marks]

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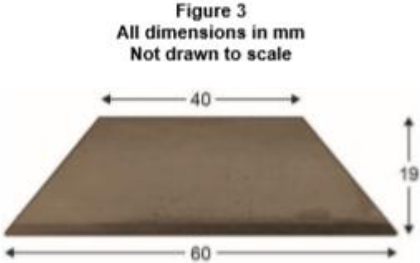
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# Answers

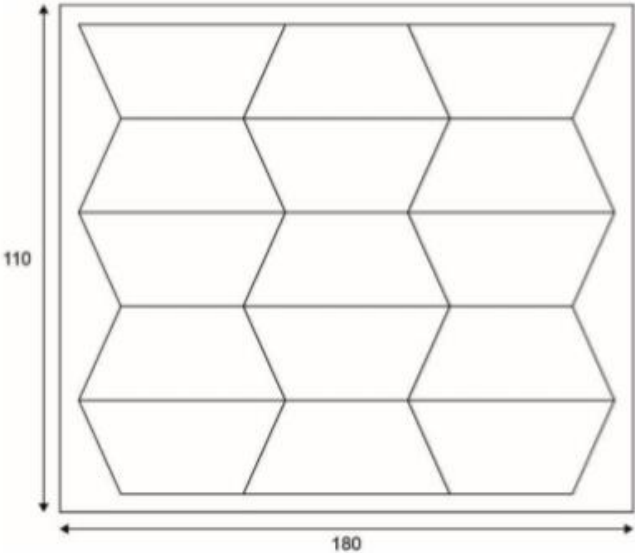
07.1

Figure 3 shows a craft knife blade.

The craft knife blade is manufactured from stainless steel in the shape of a trapezium.



The craft knife blades are cut from a sheet of stainless steel:



Calculate the percentage of the sheet that is wasted when **15** craft knife blades have been cut out.

Show your working out.

[3 marks]

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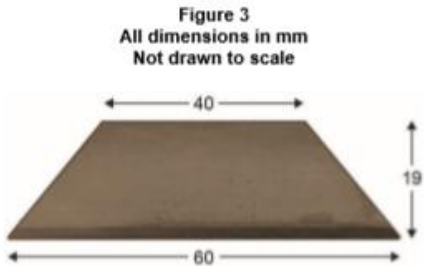
METHOD ONE		
Area of trapezium (M1)	$\text{Area} = \frac{1}{2} (a + b) \times h$ $\text{Area} = \frac{1}{2} (40 + 60) \times 19$ $\text{Area} = 950 \text{ (mm}^2\text{)}$	1 mark
Calculation of total area wasted (M2)	$= 15 \times \text{their Area of trapezium}$ $= 15 \times 950$ $= 14\,250 \text{ (mm}^2\text{)}$  $\text{Height of sheet} \times \text{width of sheet} - (15 \times \text{their area})$ $= (180 \times 110) - \text{their } 14\,250$ $= 19\,800 - 14\,250$ $= 5\,550 \text{ (mm}^2\text{)}$	1 mark
Calculation of percentage wasted (A1)	$= \frac{\text{Area of sheet} - (15 \times \text{their area})}{\text{Area of sheet}} \times 100$ $= \frac{19\,800 - 14\,250}{19\,800} \times 100$ $= 28.03 \text{ (\%)}$  $= [28, 28.03] \text{ (\%)}$	1 mark

METHOD TWO		
Area of trapezium (M1)	$\text{Area of rectangular centre} = 40 \times 19$ $= 760 \text{ (mm}^2\text{)}$  $\text{Area of triangular ends} = \frac{1}{2} \times \text{base} \times \text{height}$ $= 0.5 \times 10 \times 19$ $= 95 \text{ (mm}^2\text{)}$  $\text{Area of trapezium} = 760 + 95 + 95$ $= 950 \text{ (mm}^2\text{)}$	1 mark
Calculate %age of sheet used (M2)	$\text{Area used} = 15 \times \text{their area of trapezium}$ $= 15 \times 950$ $= 14\,250 \text{ (mm}^2\text{)}$  $\text{Area of sheet} = 180 \times 110$ $= 19\,800 \text{ (mm}^2\text{)}$  $\text{Area of sheet used} = \frac{\text{their } 14\,250}{\text{their } 19\,800} \times 100$ $= [71.96, 71.97] \%$	1 mark
Calculate %age wasted (A1)	$= 100 - \text{their } 71.97$ $= 28.03$	1 mark

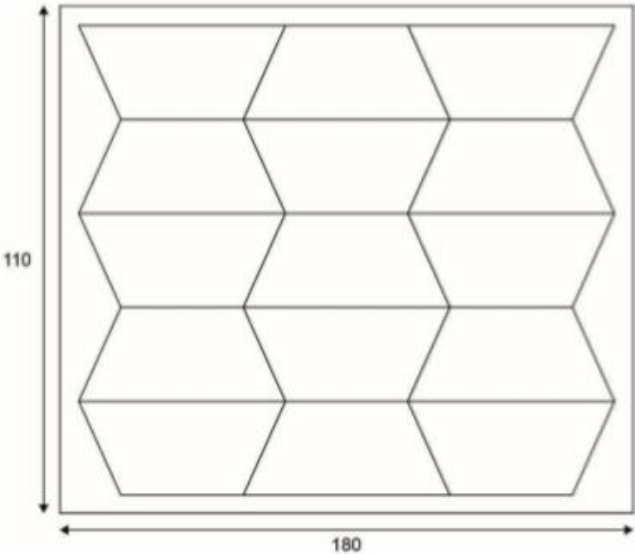
# Continued...

07.1 Figure 3 shows a craft knife blade.

The craft knife blade is manufactured from stainless steel in the shape of a trapezium.



The craft knife blades are cut from a sheet of stainless steel:



07.2

Each stainless steel sheet costs £4.25. What is the total cost of the waste material if 135 craft knife blades need to be manufactured?

Give your answer in pounds and pence. Show your working out.

[3 marks]

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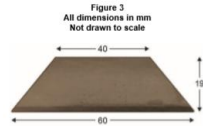
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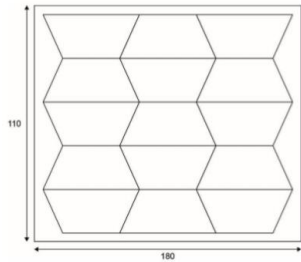
Continued... answer

**07.1** Figure 3 shows a craft knife blade.

The craft knife blade is manufactured from stainless steel in the shape of a trapezium.



The craft knife blades are cut from a sheet of stainless steel.



**07.2** Each stainless steel sheet costs £4.25. What is the total cost of the waste material if 135 craft knife blades need to be manufactured?

Give your answer in pounds and pence. Show your working out.

**[3 marks]**

[illegible]

7

2

Each stainless steel sheet costs £4.25. What is the total cost of the waste material if 135 craft knife blades need to be manufactured?

3 marks

Give your answer in pounds and pence. Show your working out.

## METHOD ONE

Calculate number of sheets required (M1)	$\frac{135}{15} = 9$	1 mark
Total cost of sheets(M2)	their $9 \times 4.25$ = (£) 38.25	1 mark
Calculate cost of waste. Answer given in pounds and pence. (A1)	$38.25 \times \frac{28}{100}$ (or their percentage waste from 8ai) = (£) 10.71	1 mark

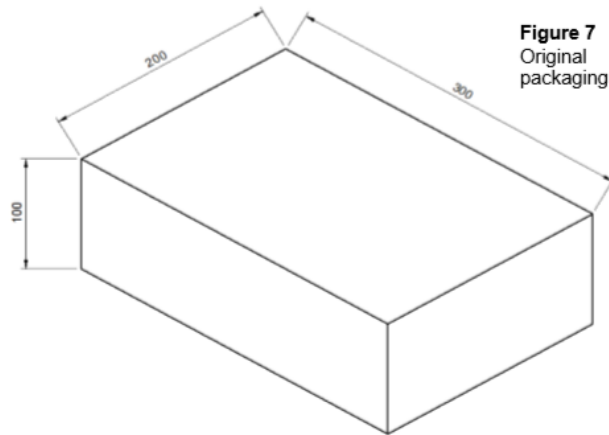
## METHOD TWO

Calculate cost of 1mm <sup>2</sup> of sheet (M1)	$\begin{aligned} \text{Area of sheet} &= 180 \times 110 \\ &= 19\,800 \text{ mm}^2 \\ \\ 4.25 \div 19\,800 &= \text{£}0.0002\,146\,464 \text{ (mm}^2\text{)} \end{aligned}$	1 mark
Cost of waste from one sheet (M2)	$\begin{aligned} 0.0002\,146\,464 \times 5550 \text{ (or their waste area from 8ai)} \\ \\ &= (\text{£})1.1912\,878\,788 \end{aligned}$	1 mark
Cost of waste from 9 sheets. Answer given in pounds and pence. (A1)	$\begin{aligned} \text{£}1.1912\,878\,788 \times 9 &= \text{£}10.7216 \\ &= (\text{£})\,10.72 \end{aligned}$	1 mark

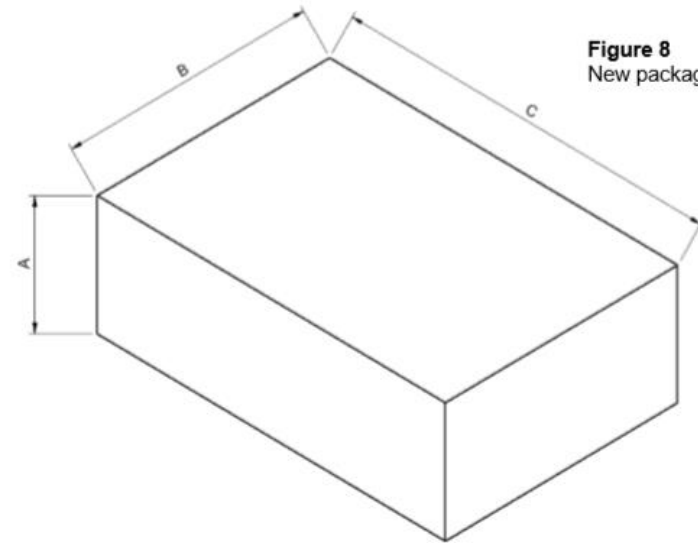
# Next question...

1 4

A video games manufacturer wants to reduce the amount of packaging for one of their products. The packaging is to keep the same proportions, but has a volume reduction of 25%.



**Figure 7**  
Original  
packaging



**Figure 8**  
New packaging

Calculate the new length of each side to 2 decimal places. Show your working.

**[4 marks]**

A \_\_\_\_\_ mm

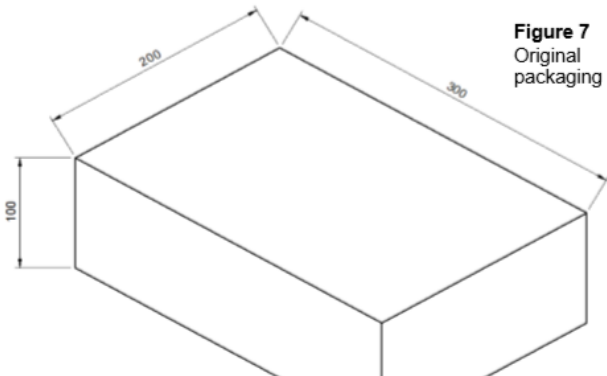
B \_\_\_\_\_ mm

C \_\_\_\_\_ mm

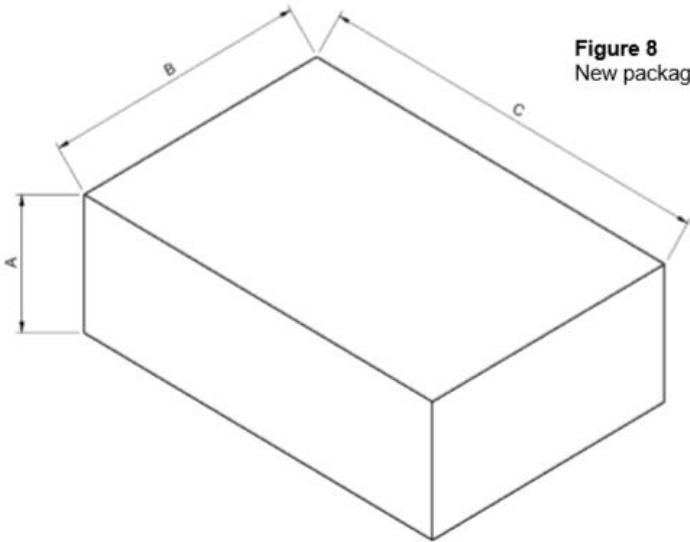
# Answers

14

A video games manufacturer wants to reduce the amount of packaging for one of their products. The packaging is to keep the same proportions, but has a volume reduction of 25%.



**Figure 7**  
Original packaging



**Figure 8**  
New packaging

14	<p>Answer requires candidate to use a volume scale factor to calculate the answer</p> <table><tr><td>Calculate existing volume of games console: <math>100 \times 200 \times 300 = 6\,000\,000\text{ mm}^3</math></td><td>1</td></tr><tr><td>b. Calculate 75% volume: <math>6\,000\,000 \times 0.75 = 4\,500\,000\text{ mm}^3</math></td><td></td></tr><tr><td>Recognition of volume scale factor as 0.75 Application of <math>\sqrt[3]{0.75}</math> to get the length scale factor: <math>= 0.90856\dots</math></td><td>1</td></tr><tr><td>Use of <math>\sqrt[3]{0.75}</math> to convert each length</td><td></td></tr></table>	Calculate existing volume of games console: $100 \times 200 \times 300 = 6\,000\,000\text{ mm}^3$	1	b. Calculate 75% volume: $6\,000\,000 \times 0.75 = 4\,500\,000\text{ mm}^3$		Recognition of volume scale factor as 0.75 Application of $\sqrt[3]{0.75}$ to get the length scale factor: $= 0.90856\dots$	1	Use of $\sqrt[3]{0.75}$ to convert each length		<p>5 marks AO42C</p>
Calculate existing volume of games console: $100 \times 200 \times 300 = 6\,000\,000\text{ mm}^3$	1									
b. Calculate 75% volume: $6\,000\,000 \times 0.75 = 4\,500\,000\text{ mm}^3$										
Recognition of volume scale factor as 0.75 Application of $\sqrt[3]{0.75}$ to get the length scale factor: $= 0.90856\dots$	1									
Use of $\sqrt[3]{0.75}$ to convert each length										

		<table><tr><td><math>A = \sqrt[3]{0.75} \times 100 = 90.86 \text{ mm}</math></td><td>1</td></tr><tr><td><math>B = \sqrt[3]{0.75} \times 200 = 181.71 \text{ mm}</math></td><td>1</td></tr><tr><td><math>C = \sqrt[3]{0.75} \times 300 = 272.57 \text{ mm}</math></td><td>1</td></tr><tr><td></td><td></td></tr></table>	$A = \sqrt[3]{0.75} \times 100 = 90.86 \text{ mm}$	1	$B = \sqrt[3]{0.75} \times 200 = 181.71 \text{ mm}$	1	$C = \sqrt[3]{0.75} \times 300 = 272.57 \text{ mm}$	1		
$A = \sqrt[3]{0.75} \times 100 = 90.86 \text{ mm}$	1									
$B = \sqrt[3]{0.75} \times 200 = 181.71 \text{ mm}$	1									
$C = \sqrt[3]{0.75} \times 300 = 272.57 \text{ mm}$	1									

# Next question...

1 5

The photograph below shows an Eames chair.



A furniture maker is manufacturing a replica of the foot stool shown above, using a one-piece foam mould and vacuum bag.

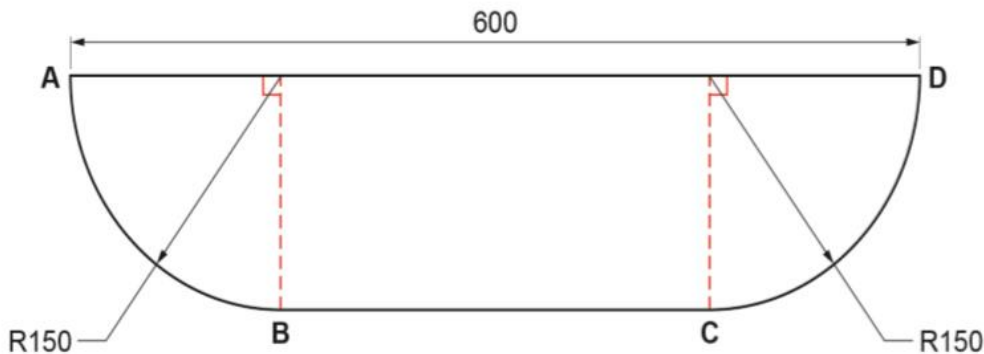


Figure 9 (foam mould)

Not drawn to scale  
All dimensions in mm

It is going to be manufactured from seven layers of 1.5mm plywood. Using the dimensioned drawing (**Figure 9**), calculate the length of plywood needed for the **outside** layer of the lamination along the length ABCD to the nearest millimetre.

[4 marks]

15

The response shows a calculation to work out an arc length or the two arcs length combined	1 mark
$2\pi \times \frac{150}{4}$ or [235.5, 236] or $2\pi \times \frac{150}{2}$ or [471, 472]	
The response shows calculations to work out the total length of the inner layer touching the foam former.	2 marks
$2\pi \times \frac{150}{4} \times 2 + 300$ or [235.5, 236] $\times 2 + 300$ or $2\pi \times \frac{150}{2} + 300$ or [471, 472] + 300	
The response shows calculations as above and some compensation for the increased radii but may use the wrong number of layers.	3 marks
The response shows <b>full</b> calculations to compensate for the increased radii due to seven layers of plywood  $R = 150 + (7 \times 1.5) = 160.5$  $2\pi \times 160.5/2 + 300 = (504.23 + 300)$ $2\pi \times \frac{160.5}{2} + 300$ or [503.97, 504.3] + 300 or [803.97, 804.3]  Outside length = 804mm (nearest millimetre)	4 marks

4  
marks  
AO42C



Next question.....

0 2

Figure 1 shows a dimension drawing of a paper weight that is to be cast in pewter.

[5 marks]

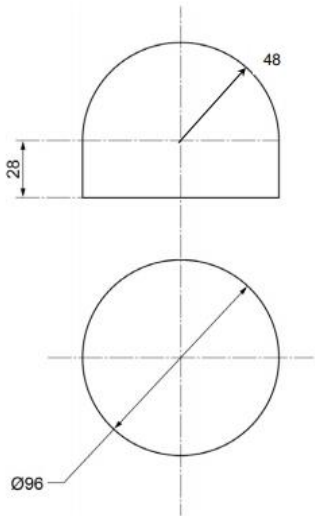


Figure 1

All dimensions in mm

The density of pewter is 7.29g/cm<sup>3</sup>. Calculate the mass of the paper weight to the nearest whole gram.

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

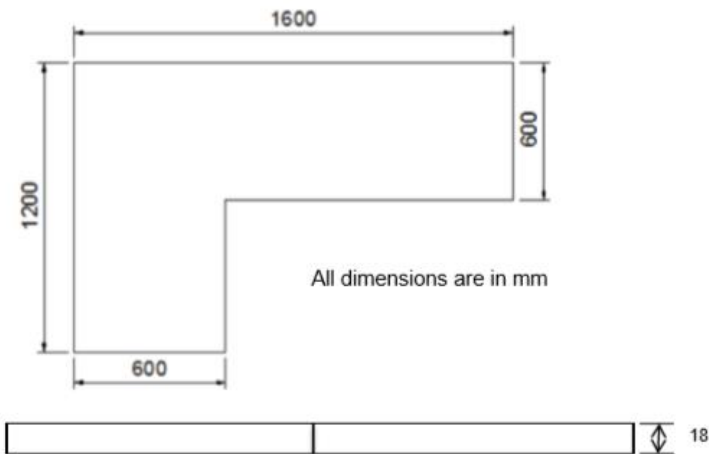
Answer \_\_\_\_\_

2			5 marks
	Volume of cylinder	$\pi r^2 h$ $3.142 \times 4.8^2 \times 2.8$ <b>202.670 (3sf)</b>	1 mark
	Volume of hemisphere	$\frac{2}{3} \pi r^3$ $\frac{2}{3} \times 3.142 \times 4.8^3$ <b>231.623(3sf)</b>	2 marks
	Total volume	$202.670 + 231.623$ <b>= 434.35cm<sup>3</sup></b>	1 mark
	Mass = Density x Volume	Mass = 7.29 X 434.35 <b>Mass =</b> <b>3166.412g(3sf)</b> <b>3166g</b>	1 mark

# Next question...

09

Figure 2 shows an office desk. The top of the office desk can be made from either solid oak or oak veneered MDF. The dimensions of the desk top are shown below.



The stock forms and prices of solid oak, oak veneered MDF and edging tape are shown in the table below.

	Solid oak	Oak veneered MDF	Edging tape
Stock Size	PAR plank 100 x 18	Sheet 2440 x 1220 x 18	50 meter roll 19mm thickness
Cost	£ 6.70 per metre	£46.60	£1.50 per metre

How much would it cost to make the table top in each of the two materials?

[6 marks]

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Oak Veneered MDF desktop cost      £ \_\_\_\_\_

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Solid oak desktop cost      £ \_\_\_\_\_

# Answers

The stock forms and prices of solid oak, oak veneered MDF and edging tape are shown in the table below.

	Solid oak	Oak veneered MDF	Edging tape
Stock	PAR plank	Sheet	50 metre roll
Size	100 x 18	2440 x 1220 x 18	19mm thickness
Cost	£ 6.70 per metre	£46.60	£1.50 per metre

How much would it cost to make the table top in each of the two materials?

[6 marks]

Oak Veneered MDF desktop cost                    £ \_\_\_\_\_

Solid oak desktop cost    £

9

<b>Veneered MDF</b>		
Area of full sheet	$2440 \times 1220 = 2.98 \text{ m}^2$	1 mark
Area of table top	$600 \times 1600 + 600 \times 600 = 1.32 \text{ m}^2$	
Cost of table top	$1.32 \div 2.98 \times 46.60 = \text{£}20.64$	1 mark
Perimeter of table top	$1600 + 1200 + 600 + 600 + 600 + 1000 = 5600 \text{ mm} = 5.6 \text{ m}$	1 mark
Edging Strip	$5.6 \times 1.5 = \text{£} 8.40$	
Total cost	$\text{£}20.64 + \text{£}8.40 = \text{£}29.04$	1 mark

<b>Solid Oak</b>		
	<b>6 planks @ 1.6m = 9.6m</b> <b>6 planks @ 0.6m = 3.6m</b>	1 mark
Total length needed	9.6 + 3.6 = 13.2m	
Total cost	13.2 × £6.70 = <b>£88.44</b>	1 mark

6  
marks  
**AO41C**

Next question...

5

Figure 2 shows a 70 mm long turned aluminium component.

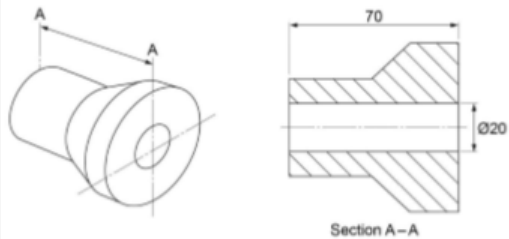
The component has a volume of 200 000 mm<sup>3</sup>.

The diameter of the through hole is increased from 20 mm to 25 mm.

Work out how much aluminium is removed as waste as a percentage of the original component.

Give your answer to two decimal places. Show your working out.

Figure 2 – all dimensions in mm



### Note

Values for  $\pi$  can be used in the range [3.14, 3.142]

Current volume of hole A	$\pi \times 10^2 \times 70$ or [21980, 21994] or 7000 $\pi$	1 mark
Volume of hole A with increased diameter	$\pi \times 12.5^2 \times 70$ [34343, 34366] or 21875 $\pi$ /2	1 mark
Difference in volume between the holes	their [34343, 34366] – their [21980, 21994] [12349, 12386]	1 mark
Difference as a percentage of the original component volume	their [12349, 12386] $\div$ 200 000) $\times$ 100 = [6.1745, 6.193] (%)	1 mark
Their answer to 2 decimal places	6.17 (%) or 6.18 (%) or 6.19 (%)	1 mark

5 marks

0	5
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Figure 2 shows a 70 mm long turned aluminium component.

The component has a volume of 200 000 mm<sup>3</sup>.

The diameter of the through hole is increased from 20 mm to 25 mm.

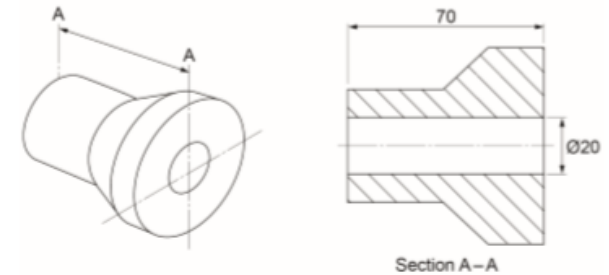
Work out how much aluminium is removed as waste as a percentage of the original component.

Give your answer to two decimal places. Show your working out.

[5 marks]

Figure 2 – all dimensions in mm

Not drawn to scale

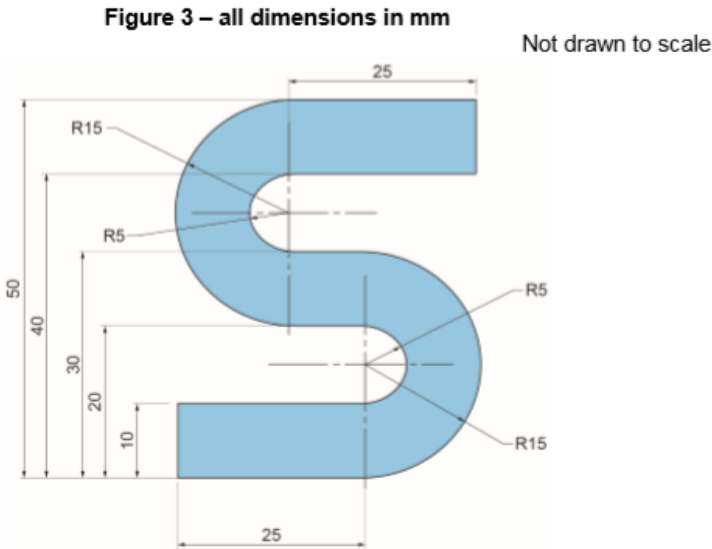


Answer \_\_\_\_\_

# Next questions...

**0 7 . 1** **Figure 3** shows a letter to be foil blocked onto packaging. The outline of the letter has straight lines and semi-circular arcs.

Calculate the surface area of the letter shown in **Figure 3**. Show your working out.  
**[2 marks]**



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Answer \_\_\_\_\_

**0 7 . 2** The dimensions of the letter shown in **Figure 3** are all increased by 50%. Work out the surface area of the enlarged letter.

Give your answer to two decimal places. Show your working out. **[2 marks]**

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# Next question...

7

1

**Figure 3** shows a letter to be foil blocked onto packaging. The outline of the letter has straight lines and semi-circular arcs.

2 marks

Calculate the surface area of the letter shown in **Figure 3**. Show your working out.

**Figure 3 – all dimensions in mm**

Not drawn to scale

Note

Values for  $\pi$  can be used in the range [3.14, 3.142]

Area of curved sections	$\pi \times 15^2 - \pi \times 5^2$ or [706, 707] – [78.5, 79] or [627, 628.5] or $200\pi$	1 mark
Total surface area	$25 \times 10 + 10 \times 10 + 25 \times 10 + [627, 628.5]$ or $600 + [627, 628.5]$ = [1227, 1228.5] ( $\text{mm}^2$ )	1 mark

7

2

The dimensions of the letter shown in **Figure 3** are all increased by 50%

2 marks

Work out the surface area of the enlarged letter.

Give your answer to two decimal places. Show your working out.

Note

Values for  $\pi$  can be used in the range [3.14, 3.142]

Area of new rectangular sections or area of curved sections	$(1.5 \times 25) \times (1.5 \times 10) + (1.5 \times 10) \times (1.5 \times 10) + (1.5 \times 25) \times (1.5 \times 10)$ or $37.5 \times 15 + 15 \times 15 + 37.5 \times 15$ or $562.5 + 225 + 562.5$ or 1350  or $600 \times 1.5^2$ or 1350  or $\pi \times 22.5^2 - \pi \times 7.5^2$ or [1589, 1591] – [176, 177] or [1412, 1415]  or $[627, 628.5] \times 1.5^2$ or [1412, 1415]	1 mark
Total surface area	$1350 + [1412, 1415] = [2762, 2765]$ or $[1227, 1228.5] \times 1.5^2 = [2762, 2765]$	1 mark

or

Alternative method Calculate scale factor	Scale factor = $1.5^2$	1 mark
Calculate new surface area	$1.5^2 \times \text{their area from 7.1}$ $2.25 \times [1227.95, 1228.4] = [2762.89, 2763.9]$	1 mark